

- 1) vypočítejte $\sigma_1, \sigma_2, \sigma_3$ a jejich polohu
- 2) určete napjatost σ, τ – izometrické roviny.

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$$\sigma_y = ((-1)^{29}) \cdot 10 + 29 \text{ MPa} = 19 \text{ MPa}$$

$$\sigma_z = (-10 \cdot 29) \text{ MPa} = -29 \text{ MPa}$$

$$\sigma_x = ((-1)^{29}) \cdot 29 + 5 \text{ MPa} = -24 \text{ MPa}$$

$$\tau_y = 30 \text{ MPa}$$

$$\tau_z = ((-1,2) \cdot (-24)) \text{ MPa} = 28,8 \text{ MPa}$$

$$\begin{bmatrix} \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \end{bmatrix}$$

$$\begin{bmatrix} \sigma_x & \tau_z & \tau_y \\ \tau_z & \sigma_y & \tau_x \\ \tau_y & \tau_x & \sigma_z \end{bmatrix} \begin{bmatrix} \cos \alpha \\ \cos \beta \\ \cos \gamma \end{bmatrix} = \begin{bmatrix} 0_x \\ 0_y \\ 0_z \end{bmatrix} \rightarrow \begin{bmatrix} -24 & -39 & 30 \\ -39 & 19 & 0 \\ 30 & 0 & 28,8 \end{bmatrix} \begin{bmatrix} \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \end{bmatrix} = \begin{bmatrix} -19,05 \\ -11,55 \\ 33,95 \end{bmatrix} \rightarrow \begin{bmatrix} \sigma^2 - 23,8\sigma^2 - 3021\sigma + 74037,6 \\ (\sigma - k_1)(\sigma - k_2)(\sigma - k_3) = 0 \end{bmatrix}$$

$$\sigma = 0_x \cos \alpha + 0_y \cos \beta + 0_z \cos \gamma = 1,93 \text{ MPa}$$

$$\tau = \sqrt{\sigma^2 - \tau^2} \approx 40,56 \text{ MPa}$$

$$\begin{bmatrix} \sigma_x - \sigma & \tau_z & \tau_y \\ \tau_z & \sigma_y - \sigma & \tau_x \\ \tau_y & \tau_x & \sigma_z - \sigma \end{bmatrix} \begin{bmatrix} \cos \alpha \\ \cos \beta \\ \cos \gamma \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \rightarrow \det = 0 \rightarrow$$

odhad k_1

σ	$f(\sigma)$	σ	$f(\sigma)$	σ	$f(\sigma)$
0	74037,6	25	-737,4	24,9	-503,289
1	70993,8	22	6704,4		
0,5	72521,275	24	1648,8		
0,1	73735,263	24,8	-268,16		
13	32939,4				

$$(\sigma^3 - 23,8\sigma^2 - 3021\sigma + 74037,6) : (\sigma - 24,8) = \sigma^2 + \sigma - 2996,2$$

$$-(\sigma^3 - 24,8\sigma^2)$$

$$1\sigma^2 - 3021\sigma$$

$$-(\sigma^2 - 24,8\sigma)$$

$$-2996,2\sigma + 74037,6$$

$$-(-2996,2\sigma + 74037,6)$$

$$-268,16$$

$$\rightarrow \sigma_1 = 24,8$$

$$\sigma_2 = 54,2$$

$$\sigma_3 = -55,2$$

$$\begin{bmatrix} 9 & 1 & 1 \\ 1 & 9 & 1 \\ 1 & 1 & 9 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

$$\begin{aligned} 1) & (\sigma_x - \sigma) \cos \alpha + \tau_z \cos \beta + \tau_y \cos \gamma = 0 \\ 2) & \tau_z \cos \alpha + (\sigma_y - \sigma) \cos \beta + \tau_x \cos \gamma = 0 \\ 3) & \tau_y \cos \alpha + \tau_x \cos \beta + (\sigma_z - \sigma) \cos \gamma = 0 \end{aligned}$$

$$\Rightarrow \cos \alpha = \frac{-\tau_z \cos \beta - \tau_y \cos \gamma}{\sigma_x - \sigma} \rightarrow 2) \cos \beta = \frac{-\tau_z P - \tau_x \cos \gamma}{\sigma_y - \sigma} \rightarrow 3) \cos \gamma = \frac{-\tau_y P - \tau_x \cos \beta}{\sigma_z - \sigma}$$

$$\Rightarrow ?$$

$$\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$

P

$$\cos \alpha = \frac{-\tau_z \cos \beta - \tau_y \cos \gamma}{\sigma_x - \sigma}$$

$$\cos \beta = \frac{-\tau_z P - \tau_x \cos \gamma}{\sigma_y - \sigma}$$

$$\cos \gamma = \frac{-\tau_y P - \tau_x \cos \beta}{\sigma_z - \sigma}$$

$$\begin{bmatrix} \sigma_x - \sigma_1 & \tau_{xz} & \tau_{xy} \\ \tau_{xz} & \sigma_y - \sigma_1 & \tau_{xy} \\ \tau_{xy} & \tau_{xz} & \sigma_z - \sigma_1 \end{bmatrix} \begin{bmatrix} \cos \alpha_1 \\ \cos \beta_1 \\ \cos \gamma_1 \end{bmatrix} = \underline{0}$$

$$\begin{bmatrix} -24-24,8 & 28,8 & 30 \\ 28,8 & 19-24,8 & 0 \\ 30 & 0 & 28,8-24,8 \end{bmatrix} \begin{bmatrix} \cos \alpha_1 \\ \cos \beta_1 \\ \cos \gamma_1 \end{bmatrix} = \underline{0}$$

$$\begin{bmatrix} -48,8 & 28,8 & 30 \\ 28,8 & -5,8 & 0 \\ 30 & 0 & 4 \end{bmatrix} \begin{bmatrix} \cos \alpha_1 \\ \cos \beta_1 \\ \cos \gamma_1 \end{bmatrix} = \underline{0} \rightarrow \left. \begin{aligned} -48,8 \cos \alpha_1 + 28,8 \cos \beta_1 + 30 \cos \gamma_1 &= 0 \\ 30 \cos \alpha_1 &+ 4 \cos \gamma_1 = 0 \\ \cos^2 \alpha_1 + \cos^2 \beta_1 + \cos^2 \gamma_1 &= 1 \end{aligned} \right\} \rightarrow$$

$$\rightarrow \textcircled{2} \cos \alpha_1 = \frac{-4 \cos \gamma_1}{30} \rightarrow \textcircled{1} -48,8 \cdot \frac{(-4 \cos \gamma_1)}{30} + 28,8 \cos \beta_1 + 30 \cos \gamma_1 = 0 \rightarrow$$

$$\rightarrow \cos \beta_1 = \frac{48,8 \frac{(-4 \cos \gamma_1)}{30} - 30 \cos \gamma_1}{28,8} \rightarrow$$

$$\rightarrow \textcircled{3} \left(\frac{-4 \cos \gamma_1}{30} \right)^2 + \left(\frac{48,8 \left(\frac{-4 \cos \gamma_1}{30} \right) - 30 \cos \gamma_1}{28,8} \right)^2 + \cos^2 \gamma_1 = 1$$

$$\left(\frac{-2 \cos \gamma_1}{15} \right)^2 + \left(\frac{-\frac{488}{75} \cos \gamma_1 - 30 \cos \gamma_1}{28,8} \right)^2 + \cos^2 \gamma_1 = 1$$

$$\frac{4}{225} \cos^2 \gamma_1 + \left(-\frac{1369}{1080} \cos \gamma_1 \right)^2 + \cos^2 \gamma_1 = 1$$

$$\frac{4}{225} \cos^2 \gamma_1 + \frac{1874161}{1166400} \cos^2 \gamma_1 + \cos^2 \gamma_1 = 1 \Rightarrow 2,62457 \cos^2 \gamma_1 = 1$$

$$\boxed{\gamma_1 = 51,9^\circ}$$

$$\cos \alpha_1 = \frac{-4 \cos \gamma_1}{30} \rightarrow \boxed{\alpha_1 = 94,7^\circ}$$

$$\cos \beta_1 = \frac{48,8 \left(\frac{-4 \cos \gamma_1}{30} \right) - 30 \cos \gamma_1}{28,8} \rightarrow \boxed{\beta_1 = 141,5^\circ}$$